## Geometric Transformation

## Story

I want a way to quickly and efficiently go from un-dispersed to dispersed images reference frame. It is therefore an ( $\mathrm{x}, \mathrm{y}$ ) ( $\mathrm{dx}, \mathrm{dy}$ ) transformation but wavelength factors in this, as well as where on the detector we are. It is therefore, in a more general way a transformation from ( $\mathrm{x}, \mathrm{y}$, lambda) ( $\mathrm{dx}, \mathrm{dy}$, lambda), where ( $x, y$ ) is the location on the detector to use to account for any field dependency.
I can thing of several things I would use this for:

- Simulating: In this case I want to be able to compute the offsets ( $\mathrm{dx}, \mathrm{dy}$ ) coordinates in the dispersed image where light originating from ( $\mathrm{x}, \mathrm{y}$ ) in the undispersed image and at a particular wavelength lambda ends up.
- Extracting: This is a reverse operation. I know the coordinates in a dispersed spectrum ( $\mathrm{x}^{\prime}, \mathrm{y}^{\prime}$ ) and therefore ( $\mathrm{dx}, \mathrm{dy}$ ) and I want to know what the wavelength of that light is since I know it originates from the pixel ( $x, y$ ) in the direct image
- In between cases: Some times, I want to be able to go back and forth from ( $x, y$,lamba) to ( $\mathrm{dx}, \mathrm{dy}$,lambda) with missing values of x , y or lambda, or $\mathrm{dx}, \mathrm{dy}$, lambda so I need functions that give me the flexibility to solve any of the in between problems, equally as fast.

I envision that I will need to compute this several millions on times so I want to keep things as fast as possible. It could be a 2D polynomial solution, which can be inverted either analytically or numerically in the case of higher polynomial orders (as in UVIS).

I want this system to be flexible and extendable to highly distorted spectra so I do not want the calibration to be dependent on the x or y coordinates, or the pathlength along the trace (which is difficult to compute and invert) or lambda directly. The choise of $x$ or $y$ is a bad one for example in cases where the spectra curve dramatically and either of these coordinates become a poor ways to measure where the trace is. Instead I want a system where each of this transformation is given as a function of an intermediate variable $t$ which can then be defined as best fit a particular disperser. Hence the functions will be dx $=f x(x, y, t) d y=f y(x, y, t)$ lambda=fl( $x, y, t$ ) and the inverse functions $x=f x^{\prime}(d x, d y, t), y=f y^{\prime}(d x, d y, t)$, lambda=fl'(dx,dy,t). The variable $t$ can be defined as $t=x$ in the case of a simple $x$-direction disperser. It can also be defined as $t=l a m b d a$, or $t=(l a m b d a-I 0) /(11-I 0)$ where $I 0$ an dl1 and the minimum and maximum wavelength in the dispersed spectrum. The latter results in $0<t<1$ which could be beneficial to some.

## Inputs

- A grism configuration file that described the transformations
- A set of coordinates and wavelenghts, etc...


## Outputs

- As set of coordinates and wavelengths, etc...


## Computations

- Computations are handles by a small module which simply implements the equation described above, using parameters values determined during the course of the instrument calibration.


## Drawbacks

- The use of the variable $t$ provides more flexibility but some bad choices can still be made. How to parametrized $t$ should be defined by balancing adequacy, speed, as well as the ability of the instrument team to calibrate the grism in that manner

